

# ***Cooperative Systems Design***

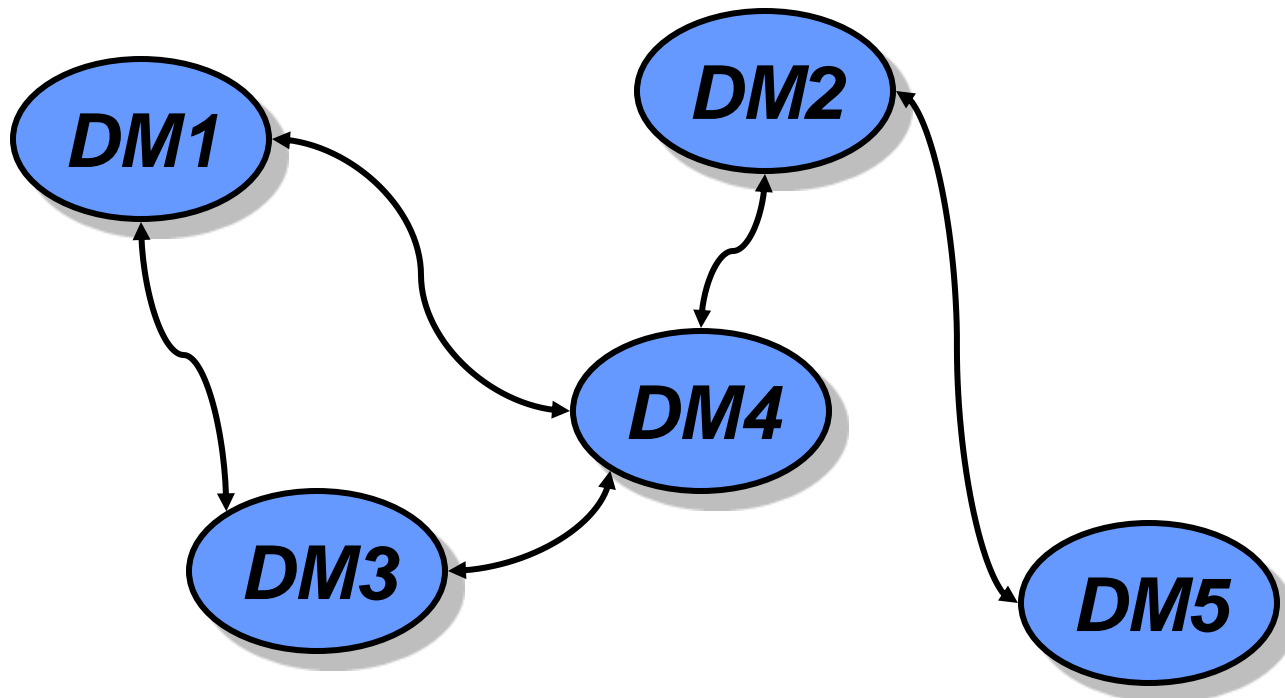
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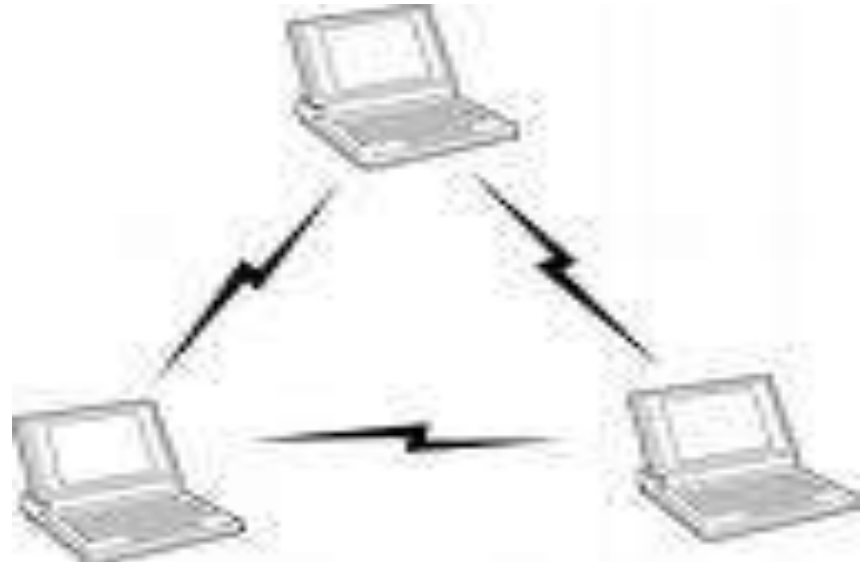
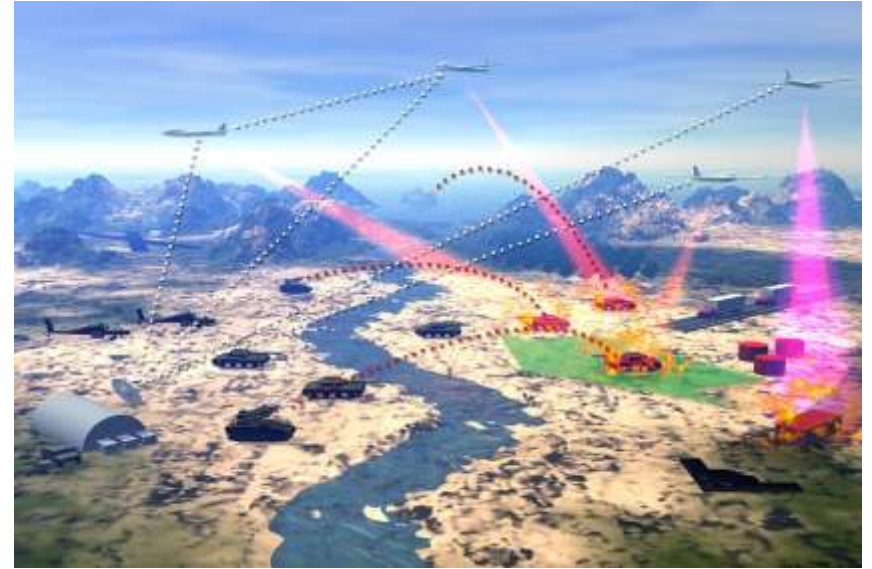
**National Science Foundation & Lockheed Martin**

# Cooperative Systems

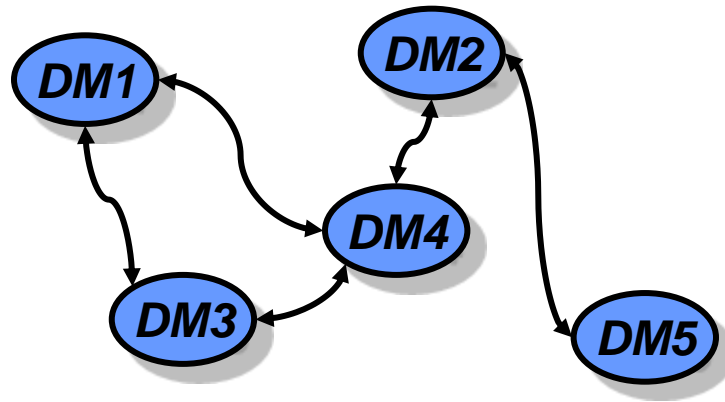


- Decision Makers (DMs) are *self-interested*
- Individual rewards depends on collective actions
- Collective behavior depends on individual actions

# Cooperative Systems: Natural and Virtual

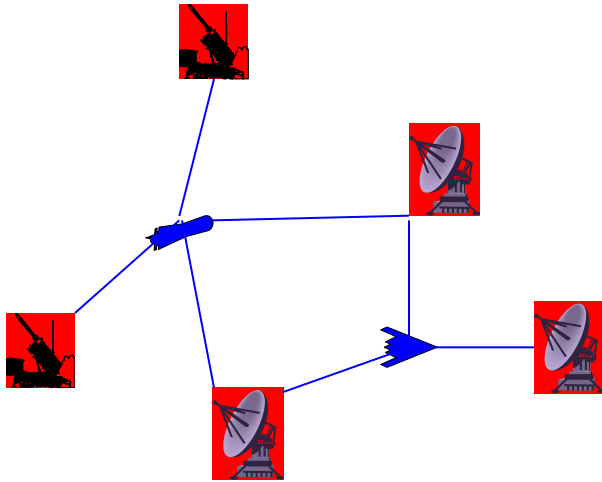


# *Cooperative Systems Design*



- Optimize a global objective through selfish DMs
- Design Problem:
  - Utility Design ( tell DMs what to optimize )
  - Negotiation Mechanism Design ( tell DMs how to optimize )

# Overview



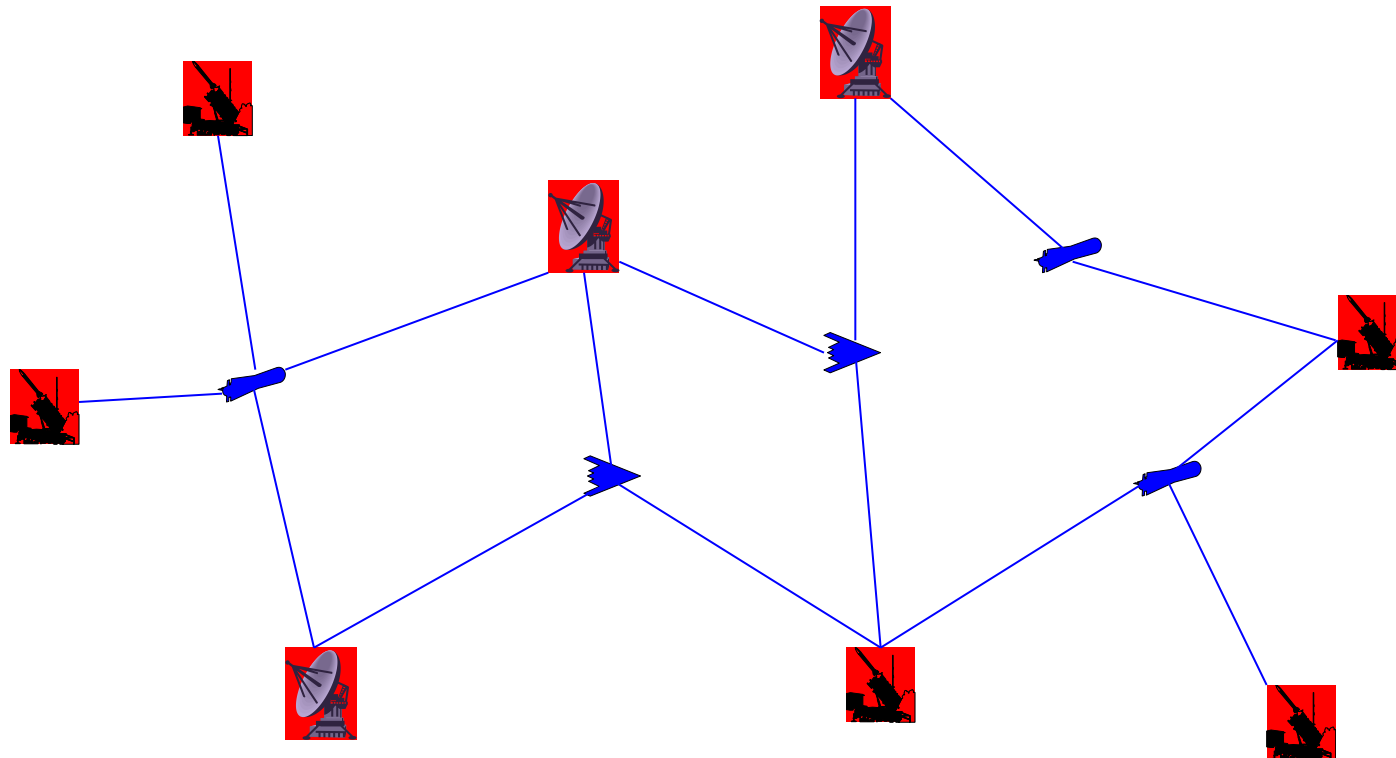
**Autonomous Target Assignment  
( MURI )**

**Cooperative Systems Design:  
A Markov Games Approach  
( NSF )**

**Autonomous Sensor Allocation  
for Submarine Tracking  
( Lockheed Martin )**

**Negotiated Signaling and Power Management  
in Wireless MIMO Interference Systems  
( UH )**

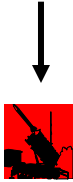
# *Setup for Target Assignment Problem*



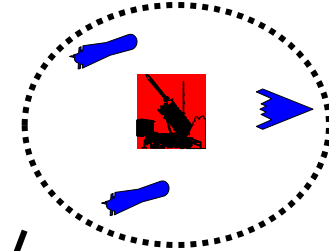
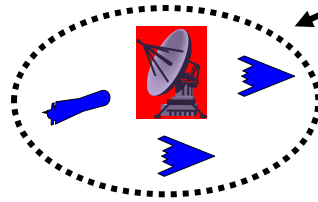
**max    Global Utility ( assignment )**

# Global Utility

No engagement here



Independent engagements

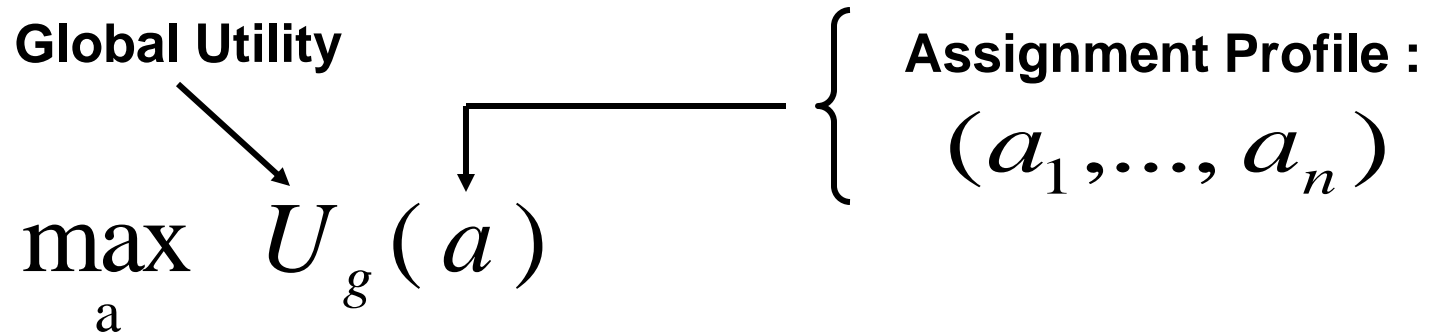


$$\text{Global Utility} = \sum_j \underbrace{\text{Utility generated at target } j}$$

↓ (for example)

$E [ \text{total value of ( destroyed target – vehicles lost ) } ]$

# ***Joint Optimization***



- **Can be formulated as an integer programming problem**
  - **Computationally hard**
  - **Relaxation techniques available for suboptimal solutions**
- **Decentralized implementation**
  - **Requires global information**
  - **Agreement issues can arise**



# ***Game Theory Formulation***

- **Vehicles are self-interested players with private utilities**

$$U_i(a)$$

- **A vehicle need not know other vehicles' utilities.**
- **Individual utilities depend on local information only.**
- **Vehicles negotiate an agreeable assignment.**

# ***Autonomous Target Assignment Problem***

## **Design**

- **Vehicle utilities**  $U_i(a)$
- **Negotiation mechanisms**

**so that**

**vehicles agree on an assignment with high Global Utility  
using**




- **low computational power**
- **low inter-vehicle communication**

# Agreeable Assignment - Nash Equilibrium

- An assignment is a ( pure ) Nash equilibrium if no player has an incentive to unilaterally deviate from it.

- Example : 

1      2      3

▲

▲

	1	2	3
1	2,1	0,0	0,0
2	0,0	1,2	0,0
3	0,0	0,0	3,3

- Pure Nash equilibria :  $(1,1), (2,2), (3,3)$
- Mixed Nash equilibria :  $([.54 \ .27 \ .18], [.27 \ .54 \ .18])$

# Utility Design

- **Vehicle utilities should be aligned with Global Utility**
- **Ideal alignment :**
  - Only globally optimal assignments should be agreeable
  - Not possible without computing globally optimal assignments
- **Relaxed alignment ( factoredness in Wolpert et al. 2000 ) :**

$$U_i(a_1, \dots, \tilde{a}_i, \dots, a_n) > U_i(a_1, \dots, a_i, \dots, a_n)$$

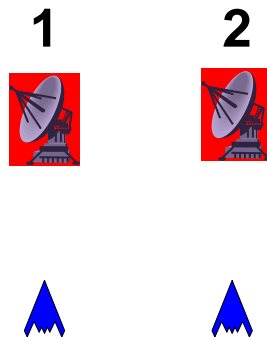
$$\Leftrightarrow$$

$$U_g(a_1, \dots, \tilde{a}_i, \dots, a_n) > U_g(a_1, \dots, a_i, \dots, a_n)$$

- Globally optimum assignment is always agreeable (pure Nash) <sub>12</sub>

# Aligned Utilities - Team Play

- For every vehicle,  $U_i(a) = U_g(a)$
- Example :



	1	2
1	2, 2	0, 0
2	0, 0	1, 1

Suboptimal Nash

- Not localized
  - Each vehicle needs global information
  - Low Signal-to-Noise-Ratio (Wolpert et al. 2000)

## *Aligned Utilities - Wonderful Life Utility (Wolpert et al. 2000)*

- **Marginal contribution of vehicle # i to Global Utility, i.e.,**

$$U_i(a) = U_g(a) - U_g(a : \underbrace{a_i = "0"}_{\text{no engagement}})$$

- **Localized :**
  - **Equal marginal contribution to engagements within range**
  - **Signal-to-Noise-Ratio is maximized**

# *Aligned Utilities - Wonderful Life Utility (Wolpert et al. 2000)*

- **Aligned :**

$$\begin{aligned} U_i(a_1, \dots, \tilde{a}_i, \dots, a_n) - U_i(a_1, \dots, a_i, \dots, a_n) \\ = \\ U_g(a_1, \dots, \tilde{a}_i, \dots, a_n) - U_g(a_1, \dots, a_i, \dots, a_n) \end{aligned}$$

- **Leads to a Potential Game with potential  $U_g(a)$**
- **Convergent negotiation mechanisms for potential games**

# *A Misaligned Utility Structure*

- **Equally Shared Utilities :**

$$U_i(a) = \frac{\text{utility generated by engagement with } a_i}{\text{number of participating vehicles}}$$

- **Hence**

$$U_g(a) = \sum_i U_i(a)$$

- **Global optimum may not be Nash agreeable**
- **A pure Nash agreeable assignment may not exist at all !**



# *Negotiation Mechanisms*

- At step  $k$ , vehicle #  $i$  proposes a target

$$a_i(k)$$

based on the past proposal profiles

$$a(1), \dots, a(k-1)$$

- Is there a reasonable negotiation mechanism that leads to a Nash equilibrium ?
- Adopt learning methods in repeated games

# Spatial Adaptive Play

- At each negotiation step, only one randomly chosen vehicle updates its proposal
- Updating vehicle proposes  $a_i$  at step  $k$  with probability

$$p_i^{a_i}(k) := P(a_i(k) = a_i)$$

which maximizes

$$p_i(k) = \arg \max_{p_i} E_{a_i \sim p_i} U_i(a_i, a_{-i}(k-1)) + \tau H(p_i)$$

# Spatial Adaptive Play

- $p_i(k)$  is given by Gibbs distribution

$$p_i^{a_i}(k) = \frac{e^{U_i(a_i, a_{-i}(k-1))/\tau}}{\sum_{a_i} e^{U_i(a_i, a_{-i}(k-1))/\tau}}$$

- For potential games, SAP induces a Markov Chain with

$$\lim_k P(a(k) = a) = \frac{e^{U_g(a)/\tau}}{\sum_a e^{U_g(a)/\tau}}$$

## *Spatial Adaptive Play*

- As  $\tau \downarrow 0$ , we have

$$\frac{e^{U_g(a)/\tau}}{\sum_a e^{U_g(a)/\tau}} \rightarrow 1 \quad \text{for } a \in \arg \max U_g(a)$$

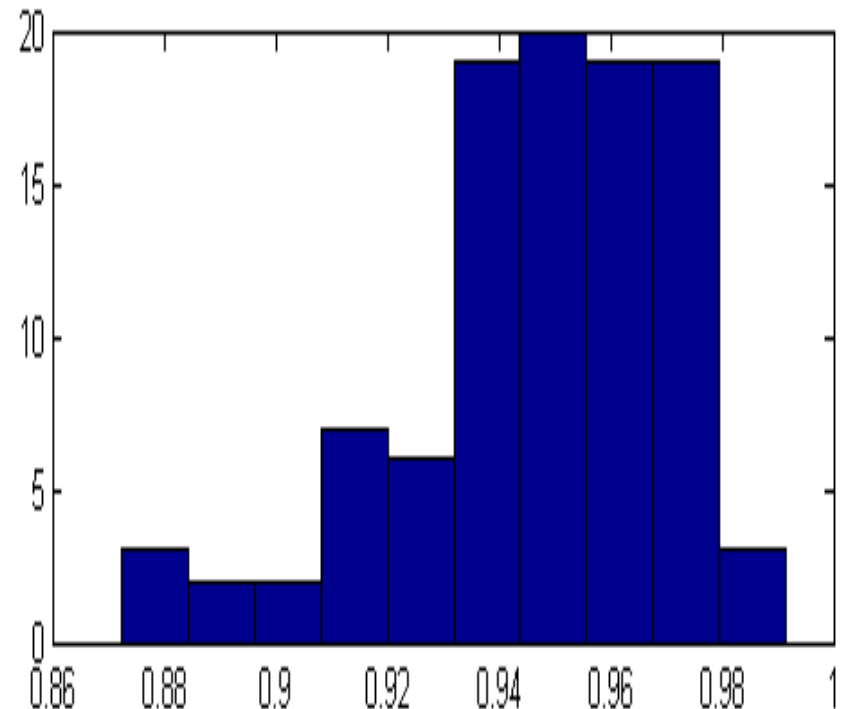
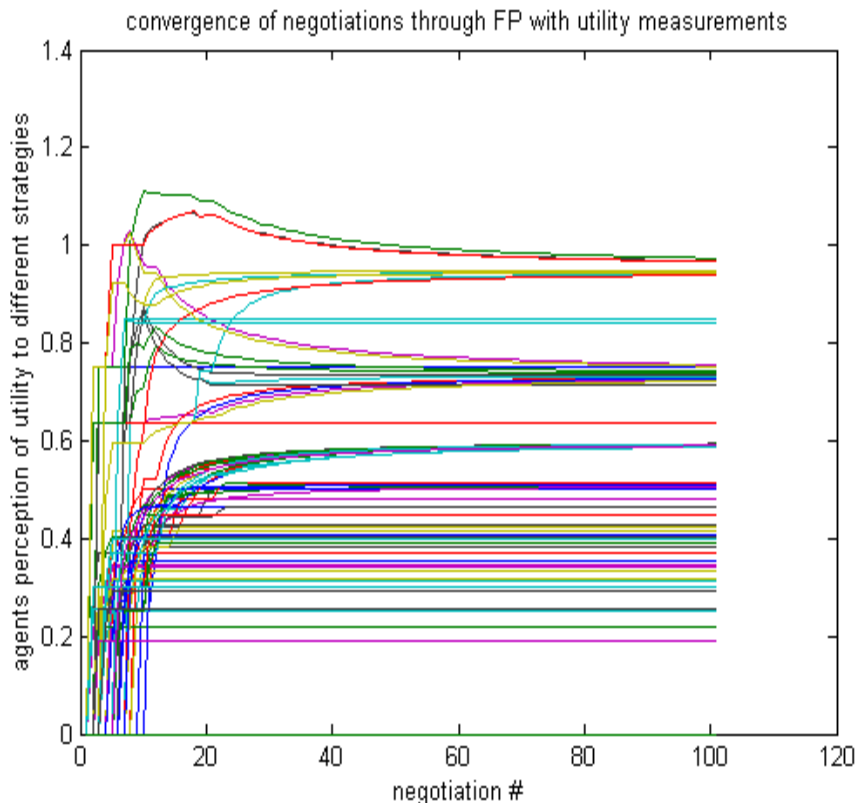
- Therefore,

$$\lim_{\tau \downarrow 0} P \left( a(\infty) \in \arg \max U_g(a) \right) = 1$$

# *Near Optimum Performance*

- Example:**

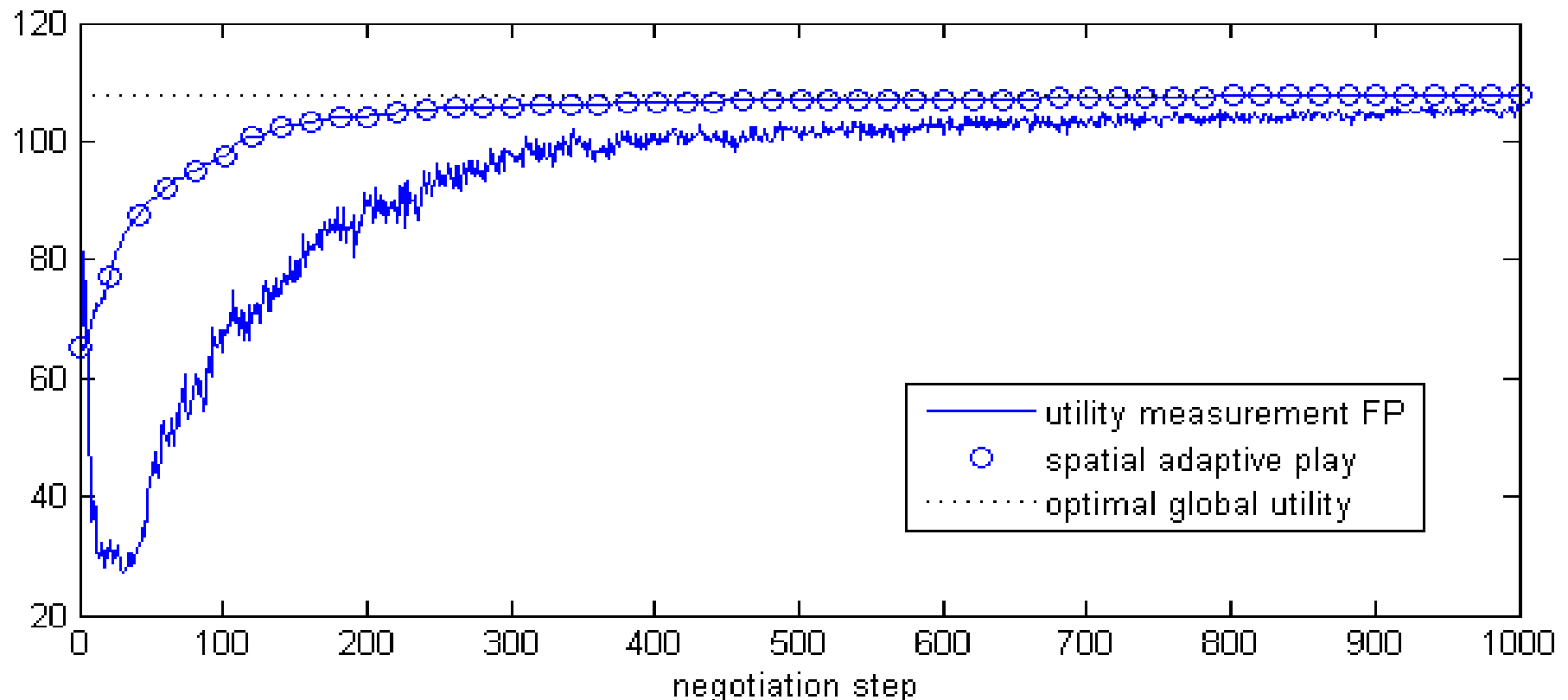
**40 uniform weapons negotiate 40 non-uniform targets**



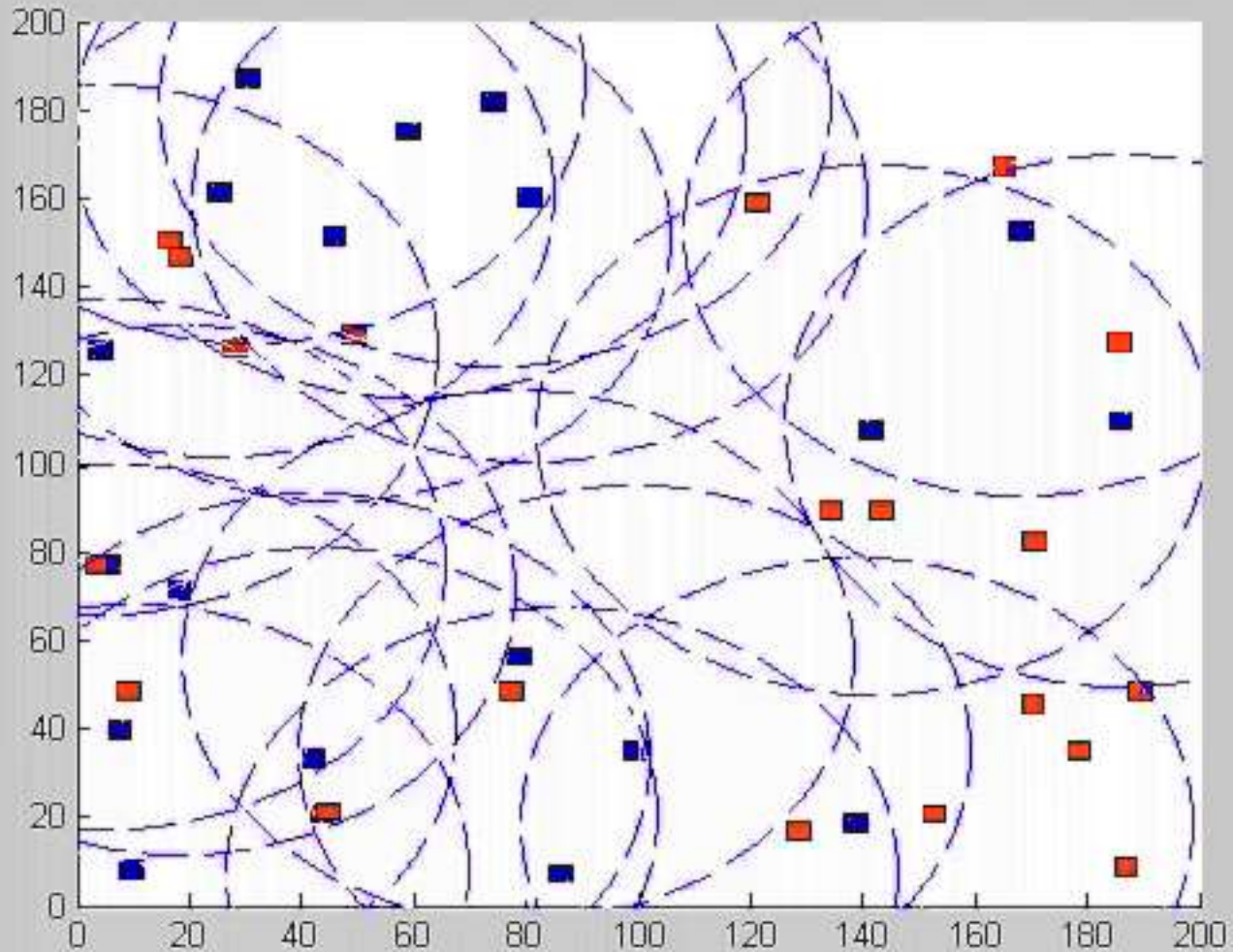
# *Near Optimum Performance*

- Example:**

**200 uniform weapons negotiate 200 non-uniform targets**

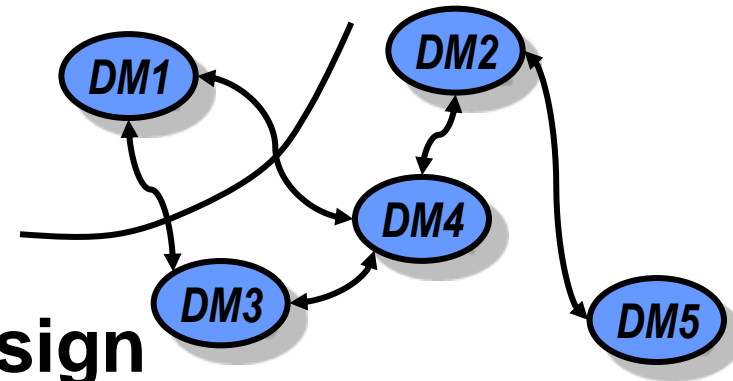


# *Greedy sequential implementation*



## *Recap and Future Work*

- **Cooperative systems design**
  - Agent utility design
  - Negotiation mechanism design
- **Multiagent systems ripe for cross disciplinary efforts**
  - Mission Planning with Autonomous Vehicles
  - Sensor Networks
  - Decentralized Inventory Control for Supply Chain Management





***Design with Look-ahead ...***  
***( ongoing work )***

# *Optimization in Dynamic & Stochastic Environments*

- Repeated decisions to optimize a long-term global utility

$$J_g = E \sum_{t=0}^T \alpha^t U_g ( a(t) , x(t) )$$

- State  $x(t)$  changes stochastically as a function of  $a(t)$
- State  $x(t)$  observed ( partially ) before choosing  $a(t)$ ,

$\Rightarrow$  optimize over CL strategies  $a(t) = \mu(x(t))$

**THANK YOU !**